

Mathematics

Geometry

9/18/2009

Foundations	Exploring the Skills and Strategies Underlying Mathematics	Using Logic and Proof to Reason Mathematically
Skills acquired by students in a previous course and refined in this course	Process Objectives Learned in the Context of Increasingly Complex Mathematical and Real-World Problems	Logic and Proof
<ol style="list-style-type: none"> 1. Apply algebraic properties (e.g., commutative, associative, distributive, identity, inverse, substitution) to simplify algebraic expressions 2. Solve single-step and multistep equations and inequalities in one variable 3. Write linear equations in standard form and slope-intercept form when given two points, a point and the slope, or the graph of the equation 4. Recognize the concept of slope as a rate of change and determine the slope when given the equation of a line in standard form slope-intercept form, the graph of a line, two points, or a verbal description 5. Graph a linear equation using a table of values, x- and y-intercepts, or slope-intercept form 6. Find the probability of a simple event 	<ol style="list-style-type: none"> 1. Apply problem-solving skills (e.g., identifying irrelevant or missing information, making conjectures, extracting mathematical meaning, recognizing and performing multiple steps when needed, verifying results in the context of the problem) to the solution of real-world problems 2. Use a variety of strategies to set up and solve increasingly complex problems 3. Represent data, real-world situation, and solutions in increasingly complex contexts (e.g., expressions, formulas, tables, charts, graphs, relation, functions) and understand the relationships 4. Use the language of mathematics to communicate increasingly complex ideas orally and in writing, using symbols and notations correctly 5. Make appropriate use of estimation and mental mathematics in computations and to determine the reasonableness of solutions to increasingly complex problems 6. Make mathematical connections among concepts, across disciplines, and in everyday experiences 7. Demonstrate the appropriate role of technology (e.g., calculators, software programs) in mathematics (e.g., organize data, develop concepts, explore relationships, decrease time spent on computations after a skill has been established) 8. Apply previously learned algebraic concepts in geometric contexts 	<ol style="list-style-type: none"> 1. Use definitions, basic postulates, and theorems about points, segments, lines, angles, and planes to write proofs and to solve problems 2. Use inductive reasoning to make conjectures and deductive reasoning to arrive at valid conclusions 3. Identify and write conditional and biconditional statements along with the converse, inverse, and contrapositive of a conditional statement; use these statements to form conclusions 4. Use various methods to prove that two lines are parallel or perpendicular (e.g., using coordinates, angle measures) 5. Read and write different types and formats of proofs including two-column, flowchart, paragraph, and indirect proofs 6. Prove that two triangles are congruent by applying the SSS, SAS, ASA, AAS, and HL congruence statements 7. Use the principle that corresponding parts of congruent triangles are congruent to solve problems 8. Use several methods, including AA, SAS, and SSS, to prove that two triangles are similar, corresponding sides are proportional, and corresponding angles are congruent 9. Use properties of special quadrilaterals in a proof

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Identifying, Classifying, and Applying the Properties of Geometric Figures in Space

- A. Points, Lines, Planes, and Space
- B. Polygons
- C. Circles
- D. Solids

Points, Lines, Planes, and Space

1. Identify and model plane figures, including collinear and noncollinear points, lines, segments, rays, and angles using appropriate mathematical symbols
2. Identify vertical, adjacent, complementary, and supplementary angle pairs and use them to solve problems (e.g., solve equations, use in proofs)
3. Identify corresponding, same-side interior, same-side exterior, alternate interior, and alternate exterior angle pairs formed by a pair of parallel lines and a transversal and use these special angle pairs to solve problems (e.g., solve equations, use in proofs)
4. Use construction techniques, including straightedge and compass, to bisect and trisect segments and to create parallel and perpendicular lines, perpendicular bisectors, and angle bisectors
5. Locate, describe, and draw a locus in a plane or space
6. Apply properties and theorems of parallel and perpendicular lines to solve problems

Polygons

1. Identify and classify triangles by their sides and angles
2. Identify medians, altitudes, perpendicular bisectors, and angle bisectors of triangles and use their properties to solve problems (e.g., find points of concurrency, segment lengths, or angle measures)
3. Apply the Triangle Inequality Theorem to determine if a triangle exists and the order of sides and angles
4. Solve problems involving the relationships formed when the altitude to the hypotenuse of a right triangle is drawn
5. Apply the Pythagorean Theorem and its converse to triangles to solve mathematical and real-world problems (e.g., shadows and poles, ladders)
6. Identify and use the Pythagorean triples in right triangles to find lengths of the unknown side
7. Identify and classify quadrilaterals, including parallelograms, rectangles, rhombi, squares, kites, trapezoids, and isosceles trapezoids, using their properties
8. Identify and classify regular and nonregular polygons (e.g., pentagons, hexagons, heptagons, octagons, nonagons, decagons, dodecagons) based on the number of sides, the angle measures, and the side lengths
9. Apply the Angle Sum Theorem for triangles and polygons to find interior and exterior angle measures given the number of sides, to find the number of sides given angle measures, and to solve real-world problems
10. Apply the Isosceles Triangle Theorem and its converse to triangles to solve mathematical and real-world problems

Circles

1. Identify and define line segments associated with circles (e.g., radii, diameters, chords, secants, tangents)
2. Determine the measure of central and inscribed angles and their intercepted arcs
3. Find segment lengths, angle measure, and intercepted arc measures formed by chords, secants, and tangents intersecting inside and outside circles
4. Solve problems using inscribed and circumscribed polygons

Solids

1. Identify and classify prisms, pyramids, cylinders, cones, and spheres and use their properties to solve problems
2. Describe and draw cross sections of prisms, cylinders, pyramids, and cones

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Comparing Congruent and Similar Geometric Figures	Using Length, Area, Perimeter, and Volume to Find Quantities and Solve Problems	Relating Geometric Ideas to the Coordinate Plane	Investigating and Applying Basic Ideas of Trigonometry
Similarity and Congruence	A. Area and Perimeter B. Lateral Area, Surface Area, and Volume	Coordinate Geometry	Introduction to Trigonometry
<ol style="list-style-type: none"> 1. Determine points or lines of symmetry and apply the properties of symmetry to figures 2. Identify congruent figures and their corresponding parts 3. Identify similar figures and use ratios and proportions to solve mathematical and real-world problems (e.g., finding the height of a tree using the shadow of the tree and the height and shadow of a person) 4. Use the definition of similarity to establish the congruence of angles, proportionality of sides, and scale factor of two similar polygons 5. Identify and draw images of transformations and use their properties to solve problems 6. Apply relationships between perimeters of similar figures, areas of similar figures, and volumes of similar figures, in terms of scale factor, to solve mathematical and real-world problems 7. Determine the geometric mean between two numbers and use it to solve problems (e.g., find the lengths of segments in right triangles) 8. Identify and give properties of congruent or similar solids 	<p>Area and Perimeter</p> <ol style="list-style-type: none"> 1. Find the perimeter and area of common plane figures, including triangles, quadrilaterals, regular polygons, and irregular figures, from given information using appropriate units of measurement 2. Manipulate perimeter and area formulas to solve problems (e.g., finding missing lengths) 3. Use area to solve problems involving geometric probability 4. Find arc lengths and circumferences of circles from given information (e.g., radius, diameter, coordinates) 5. Find the area of a circle and the area of a sector of a circle from given information (e.g., diameter, coordinates) <p>Lateral Area, Surface Area, and Volume</p> <ol style="list-style-type: none"> 1. Find the lateral area, surface area, and volume of prisms, cylinders, cones, and pyramids in mathematical and real-world settings 2. Use cross sections of prisms, cylinders, pyramids, and cones to solve volume problems 3. Find the surface area and volume of a sphere in mathematical and real-world settings 	<ol style="list-style-type: none"> 1. Use slope to distinguish between and write equations for parallel and perpendicular lines 2. Apply the midpoint and distance formulas to points and segments to find midpoints, distances, and missing information 3. Use coordinate geometry to solve problems about geometric figures (e.g., segments, triangles, quadrilaterals) 4. Write equations for circles in standard form and solve problems using equations and graphs 5. Determine the effect of reflections, rotations, translations, and dilations and their compositions on the coordinate plane 	<ol style="list-style-type: none"> 1. Apply properties of 45-45-90 and 30-60-90 triangles to determine lengths of sides of triangles 2. Find the sine, cosine, and tangent ratios of acute angles given the side lengths of right triangles 3. Use trigonometric ratios to find the sides or angles of right triangles and to solve real-world problems (e.g., use angles of elevation and depression to find missing measures)